## Angles in Polygons Answers

1. Complete the table. The first one has been completed for you.

Note: each polygon is regular.

| Polygon | Sum of Interior Angles | Interior Angle | Exterior Angle |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & (n-2) \times 180^{\circ} \\ & (3-2) \times 180 \end{aligned}$ $180^{\circ}$ | $180 \div 3$ $60^{\circ}$ | $360 \div 3$ $120^{\circ}$ |
| Rectangle | $\begin{aligned} & (n-2) \times 180^{\circ} \\ & (4-2) \times 180 \end{aligned}$ $360^{\circ}$ | $360 \div 4 \text { or } 180-90$ $90^{\circ}$ | $360 \div 4$ $90^{\circ}$ |
|  | $\begin{aligned} & (n-2) \times 180^{\circ} \\ & (5-2) \times 180 \end{aligned}$ $540^{\circ}$ | $540 \div 5 \text { or } 180-72$ $108^{\circ}$ | $360 \div 5$ $72^{\circ}$ |
|  | $\begin{aligned} & (n-2) \times 180^{\circ} \\ & (6-2) \times 180 \end{aligned}$ $720^{\circ}$ | $720 \div 6 \text { or } 180-60$ $120^{\circ}$ | $360 \div 6$ $60^{\circ}$ |
|  | $\begin{gathered} (n-2) \times 180^{\circ} \\ (7-2) \times 180 \\ 900^{\circ} \end{gathered}$ | $\begin{gathered} 900 \div 7 \text { or } 180-51.4 \\ 128.5 \dot{7} 142 \dot{8} \\ 128.6^{\circ} \end{gathered}$ | $\begin{gathered} 360 \div 7 \\ 51 . \dot{4} 28571 \\ 51.4^{\circ} \end{gathered}$ |
|  | $\begin{aligned} & (n-2) \times 180^{\circ} \\ & (8-2) \times 180 \end{aligned}$ $1080^{\circ}$ | $1080 \div 8 \text { or } 180-45$ $135^{\circ}$ | $360 \div 8$ $45^{\circ}$ |
|  | $\begin{gathered} (n-2) \times 180^{\circ} \\ (9-2) \times 180 \\ 1260^{\circ} \end{gathered}$ | $1260 \div 9 \text { or } 180-40$ $140^{\circ}$ | $360 \div 9$ $40^{\circ}$ |


|  | $(n-2) \times 180^{\circ}$ <br> $(10-2) \times 180$ | $1440 \div 10$ or $180-36$ | $360 \div 10$ |
| :---: | :---: | :---: | :---: |
| Decagon | $1440^{\circ}$ | $144^{\circ}$ | $36^{\circ}$ |

2. Work out the sum of the interior angles for a polygon with:
a. 20 sides
$(20-2) \times 180$
$3240^{\circ}$
b. 45 sides
$(45-2) \times 180$
$7740^{\circ}$
c. 100 sides
$(100-2) \times 180$
17 640
3. The interior angles of a polygon add up to $2880^{\circ}$. Work out the number of sides the polygon has.

$$
2880 \div 180=16
$$

$$
16+2=18 \text { sides }
$$

4. The interior angles of a polygon add up to $1980^{\circ}$. Work out the number of sides the polygon has.

$$
1980 \div 180=11
$$

$11+2=13$ sides
5. The interior angles of a polygon add up to $3060^{\circ}$. Work out the number of sides the polygon has.

```
3060 \div 180=17
```

$17+2$ = 19 sides
6. Calculate the size of each exterior angle in a regular polygon which has:
a. 6 sides
$360 \div 6=60^{\circ}$
b. 10 sides
$360 \div 10=36^{\circ}$
c. 15 sides
$360 \div 15=24^{\circ}$
d. 20 sides

$$
360 \div 20=18^{\circ}
$$

e. 50 sides

$$
360 \div 50=7.2^{\circ}
$$

7. A regular polygon has an exterior angle of $36^{\circ}$. Calculate the number of sides to the regular polygon.
$360 \div 36=10$ sides
8. A regular polygon has an interior angle of $175^{\circ}$. Calculate the number of sides to the regular polygon.

$$
\begin{aligned}
& 180-175=5^{\circ} \\
& 360 \div 5=72 \text { sides }
\end{aligned}
$$

## Challenge

A regular polygon has an interior angle that is five times larger than its exterior angle. How many sides does the regular polygon have?
$x+5 x=180$
$6 x=180$
$x=30$
$360 \div 30=12$ sides

## Angles in Polygons

## Prior Knowledge:

- Measuring angles.
- Substituting numbers into formulae.
- Know that angles in triangles sum to $180^{\circ}$.
- Know that angles on a straight line sum to $180^{\circ}$.

A polygon is a 2D shape which has 3 or more straight sides.
In a regular polygon, all the sides are the same length and all the angles are equal.

You need to know the names of these regular polygons and how many sides they have.


You also need to know how to find the interior and exterior angles of regular polygons.


An interior angle and its corresponding exterior angle add up to $180^{\circ}$.

## Exterior Angles

The sum of the exterior angles of a polygon is always $360^{\circ}$. In a regular polygon, to find an exterior angle, you can divide $360^{\circ}$ by the number of sides:
Exterior angle $=\frac{360}{n}$

## Interior Angles

The formula for the sum of the interior angles in a polygon, with $n$ sides, is:
Interior angle sum $=(n-2) \times 180^{\circ}$

This formula works for regular and irregular polygons. You can show how it works by dividing a polygon into triangles:


You can divide a pentagon into 3 triangles, a hexagon into 4 triangles and a heptagon into 5 triangles. Notice that, for each shape, you can find the number of triangles by taking two from the number of sides. This gives us ( $n-2$ ).

The angles in a triangle always sum to $180^{\circ}$. This means you can multiply the number of triangles, $(n-2)$, by 180 to get the total of the interior angles of the shape.

Because the angles in a regular shape are all equal, you can divide the sum of the interior angles by the number of sides to find the size of each interior angle.

Example 1: A regular hexagon is shown below. Calculate the size of the angle marked $x$.


Use the formula to find the sum of the interior angles.

$$
\begin{aligned}
(n-2) \times 180 & =(6-2) \times 180 \\
& =720^{\circ}
\end{aligned}
$$

As the hexagon is regular, all the interior angles are equal. Therefore, to find the size of the interior angle, divide the sum of the interior angles by the number of sides, 6:

$$
\begin{aligned}
x & =720 \div 6 \\
& =120^{\circ}
\end{aligned}
$$

Alternatively, the interior angle can be found by subtracting the exterior angle from $180^{\circ}$ : exterior angle $=720 \div 6$

$$
\begin{aligned}
x & =180-60 \\
& =120^{\circ}
\end{aligned}
$$

Example 2: A regular pentagon is shown below. Calculate the missing angle marked $x$.


The sum of the exterior angles for a polygon is $360^{\circ}$.

As the pentagon is regular, all the exterior angles are equal. Therefore, to find the missing angle, divide the sum of the exterior angles by the number of sides, 5 :
$x=360 \div 5$
$=72^{\circ}$

## Your turn

1. Complete the table. The first one has been completed for you. Note: each polygon is regular.


2. Work out the sum of the interior angles for a polygon with:
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c. 100 sides

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$\square$
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6. Calculate the size of each exterior angle in a regular polygon which has:
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| Rectangle |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

## Angles in Polygons

| Decagon |  |  |  |
| :--- | :--- | :--- | :--- |

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$\qquad$
$\qquad$
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$\qquad$
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$\qquad$
$\qquad$
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$\qquad$
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$\qquad$
$\qquad$
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$\qquad$
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$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

